Max. Marks: 75

1.

## **B.Sc. DEGREE END SEMESTER EXAMINATION - MARCH 2025**

## **SEMESTER 6: MATHEMATICS**

COURSE: 19U6CRMAT13: OPERATIONS RESEARCH (EL)

(Regular 2022 Admission and Supplementary 2021/2020/2019 Admissions)

Time : Three Hours

PART A

Answer any 10 (2 marks each)
Find an initial solution using NWCR

	Α	В	С	
1	2	1	3	10
2	4	5	7	25
3	6	0	9	25
4	1	3	5	30
	20	20	15	

- 2. What are the different types of method to find the initial solution of transportation problem.
- 3. Define Surplus variable.
- 4. If there are m rows and n columns in a transportation problem, what is the number of occupied cells.
- 5. Find an initial solution of the transportation problem.

	Α	В	С	D	Supply
U	19	30	50	10	7
V	70	30	40	60	9
W	40	8	70	20	18
Demand	5	8	7	14	

- 6. When does a solution become degenerate.
- 7. Find value of the game and optimum strategies for the payoff matrix;  $\begin{bmatrix} 5 & 1 \\ 3 & 4 \end{bmatrix}$
- 8. Define Maximin principle.
- 9. What is the standard form of LPP?
- 10. Identify whether the feasible region formed by the constraints  $x+y \le 4$ ,  $3x+3y \ge 18$ ,  $x \ge 0$ ,  $y \ge 0$  is bounded or unbounded.
- 11. Find the dual of

Maximize 
$$z = 2x_1 + 3x_2$$
  
Subject to  $5x_1 + 7x_2 \le 35$   
 $4x_1 + 9x_2 \le 36$ .

 $x_1, x_2$  are non negative .

12. Consider an LPP with m constraints and n variables, then what is the number of basic variables.

 $(2 \times 10 = 20)$ 

## PART B Answer any 5 (5 marks each)

- 13. Briefly explain two phase method.
- 14. Solve using graphical method

$$egin{array}{ll} ext{Minimize} & 4x_1 + 5x_2 \ ext{subject to} & x_1 + 4x_2 \geq 5 \ & 3x_1 + 2x_2 \geq 7, 3x_1 + x_2 \geq 2 \ & x_1, x_2 \geq 0, \end{array}$$

15. Construct the first two simplex table of the LPP

$$egin{array}{ll} ext{Max} & x_1+x_2 \ ext{subject to} & x_1+x_2 \leq 1 \ & 2x_1+1x_2 \leq 6 \ & x_1,x_2 \geq 0 \end{array}$$

- 16. Prove that the dual of the dual is primal.
- Use rule of dominance to reduce the payoff matrix  $\begin{bmatrix} 3 & -2 & 4 \\ -1 & 4 & 2 \\ 2 & 2 & 6 \end{bmatrix}$
- 18. Briefly explain the General Mathematical Model of Transportation problem.
- 19. Explain the algorithm to solve Assignment problems.
- 20. Write the standard form of primal and dual.

 $(5 \times 5 = 25)$ 

## PART C Answer any 3 (10 marks each)

21. Find the value of game with the given payoff 
$$\begin{bmatrix} 3 & -2 & 4 \\ -1 & 4 & 2 \\ 2 & 2 & 6 \end{bmatrix}$$

22. Obtain an optimal solution using MODI method for the following transportation problem.

	Α	В	С	D	Supply
U	19	30	50	10	7
V	70	30	40	60	9
W	40	8	70	20	18
Demand	5	8	7	14	

23. Solve using VAM

	А	В	С	
1	2	1	3	10
2	4	5	7	25
3	6	0	9	25
4	1	3	5	30
	20	20	15	

24. Explain the algorithm of Simplex method.

 $(10 \times 3 = 30)$