UNDERGRADUATE END SEMESTER EXAMINATION - OCTOBER 2024 SEMESTER 5 : MATHEMATICS (OPEN COURSE)

COURSE: 19U5OCMAT1: APPLICABLE MATHEMATICS

(For Regular 2022 Admission and Supplementary 2021/2020/2019 Admissions)

Time : Three Hours Max. Marks: 75

PART A Answer any 10 (2 marks each)

- 1. The speed of a car is 54km/hr. What is its speed in m/sec?
- 2. Find $\log_2 128$.
- 3. Find the square root of 1296.
- 4. Find the LCM of 72, 84, 126.
- 5. Which among the following is not a prime: 23, 43, 63, 83?
- 6. Write in exponential form: $\log_5 625 = 4$.
- 7. If 15 men can complete a piece of work in 90 days, in how many days will 18 men complete it?
- 8. Evaluate $\int \frac{1}{x} dx$
- 9. Evaluate $\int_0^1 e^x dx$
- 10. Divide 108 into two parts in the ratio 4:5
- 11. Differentiate xe^{2x}
- 12. Solve $8x + \frac{21}{4} = 3x + 7$

 $(2 \times 10 = 20)$

PART B Answer any 5 (5 marks each)

- 13. At a point on the level ground, the angle of elevation of the vertical tower is found to be such that its tangent is 5/12. On walking 192 meters towards the tower, the tangent of the angle of elevation is 3/4. Find the height of the tower.
- 14. Abhay lent Rs.8000 to his friend for 3 years at the rate of 5% per annum compound interest. What amount would Abhay get after 3 years?
- 15. Draw the graph of the line 3x+4y=18.
- 16. Find the greatest number that exactly divides 105, 1001, and 2436.

17. Find
$$\dfrac{dy}{dx}$$
 when $y=\left(\dfrac{x-5}{2x+1}\right)^3$

- 18. The length of a rectangle is halved and breadth is tripled. Find the percentage change in the area.
- 19. Two dice are thrown together. Find the probability that the product of the numbers on the top of the dice is:

(i) 6 (ii) 12 (iii) 7

20. John buys a vehicle for Rs.4700 and spends Rs.800 on its repairs. If he sells the vehicle for Rs.5800, then find his gain percent.

 $(5 \times 5 = 25)$

PART C Answer any 3 (10 marks each)

- 21. (a) Differentiate $x^2 log x$ with respect to x.
 - (b) Find $\int \frac{1}{x(logx)^2}$
- 22. A committee of 3 is to be formed from 6 boys and 4 girls. In how many ways can this be done so as to include
 - (i) no girls
 - (ii) exactly 1 girl
 - (iii) at least 1 girl
- 23. (a) A sum of money amounts to Rs.944 in 3 years at simple interest. If the rate of interest is raised by 25%, the sum amounts to Rs.980 during the same period. Find the sum and the rate of interest.
 - (b) Ram Singh bought a refrigerator for Rs.4000 on credit. The rate of interest for the first year is 5% and for the second year is 15%. How much will it cost him if he pays the amount after two years?
- 24. (a)If Rs. 782 be divided into three parts, proportional to 6:8:9, then find the first part, second part, and third part.
 - (b)In an election a candidate who gets 84% of the votes is elected by a majority of 476 votes. What is the total number of votes polled?

 $(10 \times 3 = 30)$