

**B. Sc. DEGREE END SEMESTER EXAMINATION : MARCH 2023****SEMESTER 6 : PHYSICS****COURSE : 19U6CRPHY13: COMPUTATIONAL PHYSICS (EL)***(For Regular - 2020 Admission and Supplementary - 2019 Admission)*

Time : Three Hours

Max. Marks: 75

**PART A****Answer any 10 (2 marks each)**

1. Briefly outline, basic Gauss elimination, in the case of a system of linear equations.
2. List the total number of operations, required for Gauss elimination method.
3. What is a stopping criterion?
4. What are analytic solutions? Are there any limitations, with such solutions?
5. Differentiate between interpolation and extrapolation.
6. What is a shift Operator? Give its 2 properties.
7. Obtain the Forward difference table for a set of 5 points.
8. Define the forward difference operator and arrive at the expression for the second forward differences.
9. Give a graphical analysis of implementing Trapezoidal rule and also mark the error involved in this calculation.
10. What is the major difference between Runge-Kutta 1st and 2nd order methods to solve 1st order Ordinary Differential Equations.
11. Discuss Taylor series method in solving 1st order Ordinary Differential Equations.
12. Give a graphical analysis of implementing Simpson's 1/3 rule and also mark the error involved in this calculation.

**(2 x 10 = 20)****PART B****Answer any 7 (5 marks each)**

13. Solve the following system of equation using simple Gauss elimination,  $x + 2y + 3z = 8$   
 $2x + 4y + 9z = 8$   
 $4x + 3y + 2z = 2$
14. Solve the following system of equation using simple Gauss elimination, with partial pivoting,  $2x + 2y + z = 6$   
 $4x + 2y + 3z = 4$   
 $x + y + z = 0$
15. Find a root of the given equation using, secant method:  $x - e^x + 2 = 0$ .
16. Show that  $\Delta(\log(x)) = \log(1+ h/x)$
17. Find the polynomial  $f(x)$  by using Lagrange's formula and hence find  $f(3)$  for  $(x,y)$ : (0,2), (1,3), (2,12) and (5,147)
18. Evaluate  $\Delta(\cos(x))$
19. From the following data sets obtain the first and second derivatives for  $x = 1.2$ 

|    |        |        |        |        |        |        |        |
|----|--------|--------|--------|--------|--------|--------|--------|
| x: | 1.0    | 1.2    | 1.4    | 1.6    | 1.8    | 2.0    | 2.2    |
| y: | 2.7183 | 3.3201 | 4.0552 | 4.9530 | 6.0496 | 7.3891 | 9.0250 |

20. Find  $y(0.2)$  for  $dy/dx = (x-y)/2$ ,  $y(0) = 1$ , with step length 0.1 using Runge-Kutta 2 method
21. Using Taylor series method, upto 3rd order, find solution for the differential equation  $y' = x-y^2$ ,  $y(0)=1$ .
22. Find  $y(0.1)$  for  $dy/dx = (x-y)/2$ ,  $y(0) = 1$ , with step length 0.1 using Runge-Kutta method  
**(5 x 7 = 35)**

**PART C**

**Answer any 2 (10 marks each)**

23. Explain bisection, false position, Newton-Raphson and secant method can be used to find roots of equations and make a comparison of the associated convergences.
24. Derive the Newton's forward interpolation formula.
25. Discuss the linearization fitting techniques to be used to solve the following non-linear laws:  $y = ae^{bx}$ ;  $xy^a = b$  and  $y = ab^x$
26. With Mathematical proof, show that Modified Euler method is more accurate than Euler method.

**(10 x 2 = 20)**