Reg. No ..... Name .....

#### 17P118

# MSc DEGREE END SEMESTER EXAMINATION- NOVEMBER 2017 SEMESTER 1 : PHYSICS COURSE : 16P1PHYT02 ; CLASSICAL MECHANICS

(For Regular - 2017 Admission)

Time : Three Hours

Max. Marks: 75

#### Section A (Objective type) Answer all the questions (1 Mark each)

- The number of degrees of freedom of a rigid body is
  (a) 2
  (b) 6
  (c) 9
  (d) 3
- 2. Which of the following equation does not represent Hamilton's principle for a conservative system
  - (a)  $\delta\int pdq=0$  (b)  $\delta\int Tdt=0$  (c)  $\delta H>0$  (d)  $\delta S=0$

3. If the generating function has the form  $F = F(q_j, P_j, t)$ (a)  $p_j = \frac{\partial F}{\partial q_j}, Q_j = \frac{\partial F}{\partial P_j}$  (b)  $p_j = \frac{-\partial F}{\partial q_j}, Q_j = \frac{\partial F}{\partial P_j}$ (c)  $p_j = \frac{\partial F}{\partial q_j}, Q_j = \frac{-\partial F}{\partial P_j}$  (d)  $p_j = \frac{-\partial F}{\partial q_j}, Q_j = \frac{-\partial F}{\partial P_j}$ 

- 4. If a rigid body is rotating with an angular velocity 'w' about an instantaneous axis through a fixed point in the body, the angular momentum vector  $\vec{J}$  about the same point
  - (a) will be always in the direction of  $\boldsymbol{w}$
  - (b) can be in the direction of  $\boldsymbol{w}$
  - (c) will always perpendicular to w'
  - (d) will never be in the direction of w.
- 5. Which of the following statement is true about chaotic systems
  - (a) chaotic systems can either be dissipative or conservative
  - (b) In dissipative systems phase-space volumes contract
  - (c) In conservative system phase space volumes are conserved
  - (d) All of these

(1 x 5 = 5)

## Section B (Short answer type) Answer any Seven (2 marks each)

- 6. Prove that the system for which the KE is conserved, moves along that path for which the time of transit is extremum.
- 7. Differentiate between conservative and dissipative systems.

- 8. For a free particle H = T and L = T. Hence from Hamilton's equations  $\dot{p} = \frac{-\partial T}{\partial q}$  and from Lagrange's equations  $\dot{p} = \frac{\partial T}{\partial q}$ . How do you reconcile the two equations?
- 9. Obtain poisson bracket  $[L_x, L_y]$ , where  $L_x$  and  $L_y$  are x and y components of angular momentum.
- 10. Explain how the method of action angle variables provides a procedure for quantization of systems.
- 11. What are principal axes and principal moment of inertia of a rigid body?
- 12. Show that a non-inertial frame is violating Newton's second law of motion.
- 13. If the rotation axis of a body is in the direction of principal axis, show that the angular velocity vector and angular momentum will be in the same direction.
- 14. What are the characteristics of a strange attractor?
- 15. Differentiate between chaotic system and an attractor.

(2 x 7 = 14)

## Section C (Problems / Short Essays) Answer any Four (5 marks each)

- 16. In a spherical pendulum the bob of mass m' is constrained to move on a spherical surface of radius R; R being the length of the pendulum. Set up the Lagrangian for the spherical pendulum and obtain the equations of motion.
- 17. Three masses  $m_1, m_2$  and  $m_3$  are attached with a spring with  $m_2$  in the middle and with  $m_1 = m_3$ . Obtain the modes of vibration of this system.
- 18. Two identical simple pendulums, each of length 'l', are connected by a light spring of force constant 'k'. If 'm' is the mass of each bob, show that the normal frequencies of the system are,  $w_1 = \sqrt{\frac{g}{l}}$  and  $w_2 = \sqrt{\frac{g}{l} + \frac{2k}{m}}$ .
- 19. A rigid body is rotating under the influence of an external torque 'N' acting on it. If 'w' is the angular velocity and T is the kinetic energy, show that  $\frac{dT}{dt} = N. w$ , in the principal axes system.
- 20. Choosing the origin at any one corner, obtain the inertia tensor of a rectangular parallelopiped of density ' $\rho$ ' and sides a, b, c. Hence deduce the inertia tensor for a cube of side 'a'.
- 21. Show how the iterates of the 2D-Baker's map form a Cantor set pattern.

(5 x 4 = 20)

#### Section D (Essays) Answer all questions (12 marks each)

22(a) Discuss calculus of variations and derive Lagrange's equations from Hamilton's principle.

- (b) Discuss calculus of variation. Show that the integeral  $I = \int_{x_1}^{x_2} f(y, y', x) dx$  is stationary, when  $\frac{d}{dx} (\frac{\partial f}{\partial y'}) \frac{\partial f}{\partial y} = 0$ , where  $y' = \frac{dy}{dx}$ .
- 23(a) Use the Hamilton-Jacobi method to determine the motion of a particle falling vertically in a unfiorm gravitational field.

OR

- (b) Obtain the equations of motion and first integrals of a particle moving in a central force field.
- 24(a) Explain the rate of change of a vector and derive an expression for the Coriolis force.

#### OR

(b) Obtain the pendulum equation by considering it as a non-linear system. Obtain the phase portrait of the pendulum also.

(12 x 3 = 36)