22P341 - S

MSc DEGREE END SEMESTER EXAMINATION - OCTOBER 2022

SEMESTER 3 : PHYSICS

COURSE : 16P3PHYT10 : COMPUTATIONAL PHYSICS

(For Supplementary - 2016/2017/2018/2019/2020 Admissions)

Time : Three Hours

Max. Marks: 75

PART A

Answer All (1 mark each)

1. Using Newton's forward interpolation formula obtain the value of y(1.6) if

	x:	1	1.4	1.8	2.2
	y:	3.49	4.82	5.96	6.5
- 4	1 \ F	4.5 \ 5.05		C	

- a) 5.54 b) 5.45 c) 5.35 d) None of the above
- 2. For operators E and μ

a) $E^2 \mu = 1/\mu$ b) $E\mu = 1/E$ c) $E\mu = \mu E$ d) $E\mu = 1$

- 3. Trapezoidal and Simpson's rules can be used to evaluate
 - (a) Double integrals (b) Differentiation

(c) Multiple Integrals (d) Divided difference

- 4. Single step methods are
 - (a) Euler, Adam, Milne (b) Euler RK method, Milne
 - (c) Euler, Modified Euler, RK method, Taylor (d) Euler, Milne, Taylor
- 5. An example of hyperbolic PDE is(a) Laplace equation (b) heat equation (c) wave equation (d) none of these

 $(1 \times 5 = 5)$

PART B

Answer any 7 (2 marks each)

- 6. Whats the difference between truncation and rounding off errors.
- 7. Show that the following relation for operators holds good: $\mu \equiv \operatorname{sqrt}(1 + \delta^2/4)$
- 8. Graphically explain trapezoidal rule of integration
- 9. Write a short note on Simpson's 3/8 rule of integration.
- 10. How does Monte Carlo integration work?
- 11. Discuss Adaptive step size R.K method.
- 12. Graphically explain what happens in modified Euler method way of solving ODE.
- 13. Discuss the type of stability conditions involved in implicit way of solving PDE
- 14. Write down the diffusion equation and represent the same in a finite difference representation.
- 15. Write down a linear second order PDE of the general form and mention the case when it reduces to an elliptical equation.

 $(2 \times 7 = 14)$

PART C Answer any 4 (5 marks each)

- 16. Using Newton's forward difference formula find the sum $S_n = 1^3 + 2^3 + 3^3 + \dots + n^3$
- 17. Determine the constants A and B by the least squares method such that y=Aexp(Bx) fits the following data:
 - x : 1.0 1.2 1.4 1.6 y : 40.170 73.196 133.372 243.02
- 18. From the following table find the value of dy/dx at the point x=1.0

X	1	1.1	1.2	1.3	1.4	1.5
Y	5.4680	5.6665	5.9264	6.2551	6.6601	7.1488

- 19. From the Taylor's Series for y(x), find y(0.1) correct to four decimal places if y(x) satisfies: dy/dx = $x - y^2$ and y(0) = 1.
- 20. Discuss explicit method of solving a PDE and the concept of stability.
- 21. Arrive at the nine point formula for Laplace equation.

(5 x 4 = 20)

PART D

Answer any 3 (12 marks each)

- 22.1. Discuss Cubic Spline Interpolation and also state the conditions it has to satisfy. **OR**
- 2. Discuss Simpson's 1/3 method and error associated with it.
- 23.1. Discuss the steps involved in obtaining the maxima and minima of a tabulated function. **OR**
 - 2. Discuss Euler and modified Euler mehods estimate its leading error term.
- 24.1. Discuss Gauss Seidel Iteration method, write an algorithm for the same. **OR**
 - 2. Discuss finite differences approximations of derivatives in solving Diffusion equation of one state variable.

(12 x 3 = 36)