

**M. Sc. DEGREE END SEMESTER EXAMINATION - APRIL 2021****SEMESTER 4 : MATHEMATICS****COURSE : 16P4MATT20EL : NUMERICAL ANALYSIS***(For Regular - 2019 Admission and Supplementary - 2018/2017/2016 Admissions)*

Time : Three Hours

Max. Marks: 75

**PART A****Answer All (1.5 marks each)**

1. Three approximate values of the number  $1/3$  are 0.30, 0.33, 0.34. Which of these is the best approximation?
2. Sum the terms : 0.1532, 15.45, 0.000354, 305.1, 8.12, 143.3, 0.0212, 0.634 and 0.1734
3. State Mean Value theorem and Rolle's theorem.
4. Define centro-symmetric equations.
5. Define well conditioned matrix.
6. Express the error obtained in polynomial interpolation with  $n+1$  values.
7. Briefly explain forward differences.
8. Prove that  $E = e^{hd}$
9. If  $y_1 = 4, y_3 = 12, y_4 = 19, y_x = 7$  find  $x$ .
10. Given  $y' - 1 = xy$  and  $y(0)=1$ . Obtain Taylor's series for  $y(x)$  and compute  $y(0.1)$  **(1.5 x 10 = 15)**

**PART B****Answer any 4 (5 marks each)**

11. Evaluate  $f(1)$  using Taylor's series for  $f(x) = x^3 - 3x^2 + 5x - 10$ .
12. Given  $f(x) = \sin x$ , construct the Taylor's series approximation of order 0 to 7 at  $x = \pi/3$  and state their absolute error.
13. Solve the system using Gauss elimination method  
 $0.0002x + 0.3003y = 0.1002$   
 $2.0000x + 3.0000y = 2.0000$
14. Find the cubic polynomial which takes the following values :  $y(1) = 24, y(3) = 120, y(5) = 336$  and  $y(7) = 720$ . Hence obtain the value of  $y(8)$ .
15. Derive Newton's backward interpolation formula.
16. Given the differential equation  $y'' - xy' - y = 0$  with the conditions  $y(0)=1$  and  $y'(0)=0$ , use Taylor's series method to determine the value of  $y(0.1)$ . **(5 x 4 = 20)**

**PART C****Answer any 4 (10 marks each)**

- 17.1. Explain the procedure to solve bisection method and hence solve  $f(x) = x^3 - 2x - 5$  correct to 3 decimal places.  
**OR**
2. Explain Gauss elimination method and solve the equations  $3x+y+2z = 3, 2x-3y-z = -3, x+2y+z = 4$ .
- 18.1. Explain LU decomposition and solve the equations  $2x+3y+z=9, x+2y+3z=6, 3x+y+2z=8$  using LU decomposition method.  
**OR**
2. Prove that the divided differences are symmetric in their arguments and that  $[x_0, x_1]$  is the first derivative of the polynomial. Explain Aitken's Scheme along with the table.

- 19.1. A solid of revolution is formed by rotating about the x axis, the area between the x axis, the lines  $x = 0$  and  $x = 1$  and a curve through the points with the following coordinates
- |   |        |        |        |        |        |
|---|--------|--------|--------|--------|--------|
| x | 0      | 0.25   | 0.50   | 0.75   | 1.00   |
| y | 1.0000 | 0.9896 | 0.9589 | 0.9089 | 0.8415 |
- Estimate the volume of the solid formed.

**OR**

2. Use predictor - corrector formulae for tabulating the solution of  $y' = x + y$ ,  $y(0)=0$ , for the interval  $0.4 < x \leq 1.0$  with  $h = 0.1$ .
- 20.1. Solve the given differential equation  $y' = 1 + y^2$  where  $y=0$  when  $x=0$  using Adam - Moulton method and compute  $y(0.8)$ , using fourth order Runge-kutta method to find the starter values.

**OR**

2. (a) Explain Picard's method of successive approximation. (b) Find the value of  $y(0.2), y(0.4), y(0.6)$ , for the given differential equation  $y' = 1 + y^2$  where  $y=0$  when  $x=0$ .  
**(10 x 4 = 40)**