M. A. DEGREE END SEMESTER EXAMINATION OCT.2020: FEBRUARY 2021

SEMESTER 1: ECONOMICS (CORE COURSE)

COURSE: 16P1ECOT05 – QUANTITATIVE TOOLS FOR ECONOMIC ANALYSIS

(For Regular - 2020 admission and Supplementary 2019 / 2018 / 2017 / 2016 admissions)

Time: Three Hours Max Mark: 75

PART A

Answer any eight questions. Each question carries 2 marks

- 1. Give any two uses of matrix or determinants in Economics.
- 2. Define singular matrix and give an example of it.
- 3. What do you mean by a consistent system of equations?
- 4. What is Cobb-Douglas production function?
- 5. Define a definite integral. Give one application of definite integral in Economics.
- 6. What are the conditions for a function f(x,y) to be a maximum?
- 7. How will you obtain the total revenue function from the marginal revenue function?
- 8. Define consumer's surplus.
- 9. What is trapezoidal rule?
- 10. What do you mean by feasible solution in linear programming?
- 11. What is duality theorem?
- 12. Mention the uses of input/output analysis.

 $(2 \times 8 = 16)$

PART B

Answer any Seven questions. Each question carries 5 marks

13. If
$$A = \begin{bmatrix} -4 & 1 & 3 \\ 2 & 5 & -1 \\ 6 & 9 & 3 \end{bmatrix}$$
 and $B = \begin{bmatrix} -4 & 2 & 7 \\ -2 & 1 & 5 \\ 3 & 2 & 4 \end{bmatrix}$, then verify whether $AB = BA$.

14. If A =
$$\begin{bmatrix} 1 & 0 & -1 \\ 2 & 1 & 3 \\ 3 & 1 & 4 \end{bmatrix}$$
 then find the inverse matrix of A.

- 15. Explain the significance of Euler's theorem with the help of an example of a homogeneous production function.
- 16. The utility function of a consumer is given by $f(x,y) = 2 x^3 y + 3 x y^2$. Find the marginal utilities and also show that $f_{xy} = f_{yx}$
- 17. Find the total differential of $u = x^3-5xy + 2y^3$
- 18. Minimise cost if the cost function of a firm is $C(x) = 5x^2 + 2xy + 3y^2 + 800$ subject to the production quota x + y = 39.

19. Integrate the following functions

(i)
$$8x(x^2 + 1)^3$$
 (ii) $x e^{2x}$

- 20. Explain Simpson's one-third rule.
- 21. What do you mean by the dual of a linear programming problem? Explain the dual advantages
- 22. Explain Cobb Douglas production function.

 $(5 \times 7 = 35)$

PART C

Answer any two questions. Each question carries 12 marks

23. Solve the following system of equations using matrix inverse method

$$4x + y + 2z = 7$$

$$7x - y + z = 7$$

$$3x + 4y + z = 8$$

- 24. Explain the various applications of partial derivatives in economics.
- 25. If total cost function is $C=5000+1000q-500q^2+(2/3)q^3$. Find the output at which marginal cost would be equal to the average variable cost.
- 26. A manufacturing company makes two models A and B of a product. Each piece of Model A requires 7 labour hours for fabricating and 1 labour hour for finishing. Each piece of Model B requires 8 labour hours for fabricating and 2 labour hours for finishing. For fabricating and finishing, the maximum labour hours available are 160 and 25 respectively. The company makes a profit of Rs 6000 on each piece of model A and Rs 10000 on each piece of Model B. How manypieces of Model A and Model B should be manufactured per week to realize a maximum profit? What is the maximum profit per week?

 $(12 \times 2 = 24)$
