

M. Sc DEGREE END SEMESTER EXAMINATION - JULY 2021**SEMESTER 2 : PHYSICS****COURSE : 16P2PHYT08 : THERMODYNAMICS AND STATISTICAL MECHANICS***(For Regular - 2020 Admission & Supplementary - 2019/2018/2017/2016 Admissions)*

Time : Three Hours

Max. Marks: 75

PART A**Answer All (1 mark each)**

- Entropy of the system tends to zero at:
 - $T = 0$ degrees
 - $T = \infty$
 - $T = 0$ K
 - none
- When 3 dice are thrown $125/216$ is the probability of getting:
 - One six
 - at least one six
 - 2,3,6 combination
 - none
- For free gas atoms in a cube of volume 'V'. If U is the average energy, $PV =$
 - $2U/3$
 - $3U/2$
 - UT
 - none of the above
- What is the thermodynamic quantity whose value is related to the magnitude of fluctuations of energy?
 - The pressure.
 - The heat capacity at constant volume.
 - Temperature.
 - none of these
- A plot of pressure vs. temperature for a given substance showing the various phases possible for that particular substance.
 - Phase diagram
 - P-T diagram
 - Wein Diagram
 - Histogram
(1 x 5 = 5)

PART B**Answer any 7 (2 marks each)**

- Show that for a single mole of an ideal gas $C_p = C_v + R$.
- What is a Gibbs Ensemble?
- Write down the expression for Gibbs free energy.
- Write down the expression for Helmholtz free energy.
- Obtain C_v for a diatomic gas
- Obtain the partition function for a diatomic having rotational motion alone.
- Write down the partition function of an ordinary hydrogen atom which is a mixture of ortho and para hydrogens.
- What is Wein's displacement law?
- What is meant by Fermi Surface?
- Discuss Fermi distribution function at absolute zero via plot.

(2 x 7 = 14)**PART C****Answer any 4 (5 marks each)**

- Assume that the heat capacity at constant volume of a metal varies as $(aT + bT^3)$ for low temperature. Calculate the variation of the entropy with temperature.
- A current of 0.5A flows through a 2Ω resistor for 100sec. The system whose initial temperature is 300K is thermally isolated. The heat capacity of the resistor is 0.24JK^{-1} ; for a wide range of temperatures. The temperature of the resistor changes appreciably. What is the entropy change of the system?
- The average kinetic energy $(=3k_B T/2)$ of hydrogen atoms in a stellar gas is 1eV. What is the ratio of the number of atoms in the second excited state ($n=3$) to the number in the ground state ($n=1$)? The energy levels of the hydrogen atoms are $e_n = -a/n^2$ where $a=13.6$ eV, and the degeneracy of the nth level is $2n^2$.

19. A system of particles occupying single-particles states and obeying Boltzmann statistics is in thermal contact with a heat bath at temperature T. The populations are 3.1% for 0.0281 eV; 8.5% for 0.0195 eV; 23% for 0.0109 eV; 63% for 0.0023 eV. What is the temperature of the system?
20. Obtain the Fermi wave vector for conduction electrons in lithium having a number density of $4.6 \times 10^{28} m^{-3}$.
21. In sodium there are about 2.6×10^{28} conduction electrons per cubic meter which behave as a free electron gas. From these facts estimate the Fermi energy of the gas and an approximate value of the molar specific heat capacity at 300 K

(5 x 4 = 20)

PART D

Answer any 3 (12 marks each)

- 22.1. Obtain the expression for Entropy in a canonical system.

OR

2. Obtain the expression for heat capacity of a single 2 level system.

- 23.1. Obtain the expression for density of states for a single free particle in 3 Dimension.

OR

2. Derive Sackur-Tetrode formula for entropy of an ideal gas.

- 24.1. Discuss the conditions for chemical equilibrium in terms of Gibbs free energy by taking an example

OR

2. Derive the probability distribution for a grand canonical ensemble.

(12 x 3 = 36)