

**B. Sc. DEGREE END SEMESTER EXAMINATION OCTOBER/NOVEMBER 2018****SEMESTER –5: PHYSICS (CORE COURSE)****COURSE: 15U5CRPHY05: CLASSICAL AND QUANTUM MECHANICS***(Common for Regular 2016 admission & Supplementary 2015 & 2014 admissions)*

Time: Three Hours

Max. Marks: 60

**PART A** (Very short answer questions)*Answer all questions. Each question carries 1 Mark*

- For a pendulum with an extensible string, the constraint belongs to which type?  
(a) dissipative (b) nonholonomic (c) rheonomic (d) scleronomic
- If Lagrangian is not an explicit function of time, the quantity remaining conserved is  
(a) Hamiltonian (b) linear momentum (c) angular momentum (d) time
- The dimension of action is same as that of  
(a) linear momentum (b) angular momentum (c) energy (d) acceleration
- Rayleigh-Jeans law matches with Planck's law at  
(a) low frequencies (b) high frequencies (c) all frequencies (d) none of these
- The dual behavior of electrons is  
(a) only a theory (b) an experimental fact (c) an artifact (d) meaningless
- For a wave function to be normalizable, the norm is to be  
(a) finite (b) infinite (c) zero (d) complex
- When the number of waves forming a wave packet is increased, what happens to the width of the wave packet?  
(a) becomes wider (b) becomes narrower (c) becomes zero (d) becomes infinity
- The quantum mechanical operator for momentum is  
(a)  $-i\hbar \frac{\partial}{\partial x}$  (b)  $i\hbar \frac{\partial}{\partial x}$  (c)  $-i\hbar \frac{\partial}{\partial t}$  (d)  $i\hbar \frac{\partial}{\partial t}$
- An eigen function of the operator  $i \frac{\partial}{\partial t}$  is  $e^{-i\omega t}$ . What is the corresponding eigen value?  
(a)  $\omega$  (b)  $i\omega$  (c)  $i\omega t$  (d)  $t$
- For a rigid rotator,  
(a) The energy levels are equally spaced (b) energy levels are un-equally spaced  
(c) ground state energy is non-zero (d) none of these (1 x 1 0 = 10)

**PART B (Short answer)**

Answer **any Seven** questions. Each question carries **2 Marks**

11. What do you mean by a cyclic co-ordinate? What is the nature of the conjugate momentum?
12. State the Hamilton's principle for a conservative system.
13. Compare Lagrange's and Hamilton's equations of motion.
14. What is the importance of Davisson-Germer experiment?
15. What do you mean by the expectation value of an operator? Give an expression for the same.
16. What do you mean by a stationary state?
17. Distinguish between the terms phase velocity and group velocity. Give expressions for the same.
18. What are the eigen functions and eigen values of the operators  $L^2$  and  $L_z$ ?
19. Explain the term degeneracy of eigen functions. (2 x 7 = 14)

**PART C (Problem/Derivations)**

Answer **any Four** question. Each question carries **4 Marks**

20. Obtain the equation of motion of a one-dimensional harmonic oscillator employing Lagrangian formalism.
21. Using Euler-Lagrange equation, prove that the shortest distance between two points is a straight line.
22. An X-ray beam of wavelength 1 pm suffers Compton scattering from a target. Estimate the maximum and minimum wavelength of the scattered X-rays.
23. Estimate the de Broglie wavelength of an electron which is accelerated through a potential difference of 100 V.
24. Find the expectation value of the momentum of a particle enclosed in a one-dimensional box.
25. Verify the commutation relation  $[L_x, L_y] = i\hbar L_z$ . (4 x 4 = 16)

**PART D (Long answer questions)**

Answer **any Two** question. Each question carries **10 Marks**

26. Obtain the Lagrange's equation of motion for a conservative system from D'Alembert's Principle.
27. Derive the least action principle for a conservative system.
28. What are the important conclusions of photoelectric effect? Give explanations for these effects based on Einstein's photoelectric equation.
29. Obtain the Schrödinger equation for a one-dimensional simple harmonic oscillator. Give expression for the energy eigen values. Plot the corresponding eigen functions. (10 x 2 = 20)