## B. Sc. DEGREE END SEMESTER EXAMINATION - OCTOBER 2019 SEMESTER - 3: MATHEMATICS

## (CORE COURSE FOR B. Sc. MATHEMATICS AND B. Sc. COMPUTER APPLICATIONS) COURSE: 15U3CRMAT3-15U3CRCMT3, CALCULUS

(For Regular-2018 Admission and Supplementary / Improvement 2017, 2016, 2015, 2014 Admissions) Time: Three Hours

Max Marks: 75

## PART - A

Answer all questions. Each question carries 1 mark.

1. Find $\frac{d^{2} y}{d x^{2}}$ if $x=a t^{2}, y=2$ at
2. Check the concavity of the function $y=\sin x$ over $(0, \pi)$.
3. How many asymptotes a closed curve has?
4. Define critical point of a function.
5. Find $\frac{\partial f}{\partial y}$ for $\mathrm{f}(\mathrm{x}, \mathrm{y})=\mathrm{e}^{\mathrm{x}+\mathrm{y}+1}$
6. Evaluate $\int_{0}^{3} \sqrt{y+1} d y$
7. What is the area of the surface generated by revolving the smooth curve $y=f(x)$ from $x=c$ to $x=d$ ?
8. Write the shell formula for finding the volume of the solid generated by revolving a region about the $y$-axis.
9. What is the area of a closed bounded region $R$ in polar co-ordinates?
10. Write the co-ordinate conversion formula from spherical to rectangular co-ordinates.
$(1 \times 10=10)$
PART - B
Answer any 8 questions. Each question carries 2 marks.
11. Find the nth derivative of $\cos (a x+b)$
12. Find the points of inflections of the curve $y=(\log x)^{3}$
13. Find $f_{x}$ and $f_{y}$ of $f(x, y)=x^{2}+3 x y+y-1$ at $(4,-5)$
14. Draw a tree diagram for $\frac{d z}{d t}$ for $\mathrm{z}=\mathrm{f}(\mathrm{x}, \mathrm{y}) ; \mathrm{x}=\mathrm{g}(\mathrm{t}), \mathrm{y}=\mathrm{h}(\mathrm{t})$
15. Find the local extreme values of $f(x, y)=x^{2}+y^{2}$
16. Find the area of the region enclosed by the co-ordinate axes and the line $x+y=2$
17. Find the volume of the solid generated by revolving the region bounded by $\mathrm{y}=\sqrt{x}, 0 \leq \mathrm{x} \leq 4$ and the $x$-axis about the $x$-axis
18. Change to polar integral and evaluate $\int_{0}^{1} \int_{0}^{\sqrt{1-y^{2}}}\left(x^{2}+y^{2}\right) d x d y$
19. Find the Jacobian of the transformation $x=u \cos v, y=u \sin v$
20. Evaluate $\int_{0}^{1} \int_{0}^{1-y} \int_{0}^{2} d x d z d y$

## PART - C

Answer any 5 questions. (Each question carries 5 marks)
21. Expand $\log (1+x)$ in ascending powers of $x$
22. Find the radius of curvature of the curve $\sqrt{x}+\sqrt{y}=\sqrt{a}$ at the point $\left(\frac{a}{4}, \frac{a}{4}\right)$
23. Find $\frac{\partial w}{\partial r}$ and $\frac{\partial w}{\partial s}$ in terms of $r$ and $s$ if $w=x^{2}+y^{2}: x=r-s, y=r+s$ using chain rule
24. Find the area between the curves $x+y^{2}=0$ and $x+3 y^{2}=2$
25. Find the length of the curve $y=(x / 2)^{2 / 3}$ from $x=0$ to $x=3$
26. Evaluate the integral $\int_{0}^{2 \sqrt{\ln 3}} \int_{\frac{y}{2}}^{\sqrt{\ln 3}} e^{x^{2}} d x d y$ by reversing the order of integration.
27. Evaluate the cylindrical co-ordinate integral $\int_{0}^{2 \pi} \int_{0}^{\frac{\theta}{2 \pi}} \int_{o}^{3+24 r^{2}} d z r d r d \theta$

## PART - D

Answer any 2 questions. (Each question carries 12 marks)
28. a) If $y=\left(\sin ^{-1} x\right)^{2}$, show that $\left(1-x^{2}\right) y_{n+2}-(2 n+1) x y_{n+1}-n^{2} y_{n}=0$
b) Find the evolute of the parabola $y^{2}=4 a x$
29. a) Find $\frac{d w}{d t}$, given $w=z-\sin x y$ : $x=t, y=\log t, z=e^{t-1}$
b) Find the maximum and minimum values of the fuction $f(x, y)=3 x+4 y$ on the circle $x^{2}+y^{2}=1$
30. a) Find the volume of the solid generated by revolving the region between the parabola $x=y^{2}+1$ and the line $x=3$ about the line $x=3$
b) Find the area of the surface generated by revolving the curve $x=a t^{2}, y=2 a t, 0 \leq t \leq 1$ about the $x-$ axis
31. a) Find the volume of the solid bounded by the paraboloid $z=x^{2}+y^{2}$ and below by the triangle enclosed by the lines $y=x, x=0$ and $x+y=2$ in the $x y$ - plane
b) Find the volume of the ice cream cone $D$ cut from the solid sphere $\rho \leq 1$ by the cone $\phi=\frac{\pi}{3}$

