B. Sc. DEGREE END SEMESTER EXAMINATION - OCTOBER 2019 SEMESTER - 1: COMPLEMENTARY FOR BSC PHYSICS / BSC CHEMISTRY

COURSE –19U1CPMAT1: CALCULUS - 1

(For Regular - 2019 Admission)

Time: Three Hours

Max Marks: 75

PART - A

Answer any 10 questions. Each question carries 2 marks.

- 1. State Mean Value Theorem.
- 2. Find the absolute extrema of $f(x) = x^2$ on [-2,1].
- Find the function f(x) whose derivative is 'sin x' and whose graph passes through the point [0,2].
- 4. Find the first order partial derivatives of f , when $f(x,y) = x \tan^{-1}(xy)$.
- 5. Show that $z = \ln \sqrt{x^2 + y^2}$ satisfy the Laplace equation.
- 6. Find the greatest and smallest values that the function f(x, y) = xy takes on the ellipse

$$\frac{x^2}{8} + \frac{y^2}{2} = 1$$

- 7. Find the Volume of the solid obtained by rotating the region bounded by $y = x^3$, y = 8, x = 0 about y-axis
- 8. Find the length of the asteroid $x = cos^3 t$, $y = sin^3 t$, $0 \le t \le 2\pi$
- 9. Find the area of the surface swept out by revolving the circle $x^2 + y^2 = 1$ about the x-axis.
- 10. Evaluate $\int_{0}^{1} \int_{0}^{1-y} \int_{0}^{2} dx \, dz \, dy$.
- 11. Write the Jacobian determinant of x = g(u,v), y = h(u,v).
- 12. Find the average value of f(x,y)= x (cosxy) over the rectangle $0 \le x \le \pi$ and $0 \le y \le 1$.

(2 x 10 = 20)

PART - B

Answer any five questions. Each question carries 5 marks

- 13. Does the function $f(x) = \sqrt{x(1-x)}$ on [0, 1] satisfy the hypothesis of mean value theorem?
- 14. Show that $y = \tan x$ is increasing in every interval in its domain.
- 15. Find all local maxima, local minima and saddle point of $f(x, y) = x^3 + y^3 3x 12y + 20$
- 16. The plane x + y + z = 1 cuts the cylinder $x^2 + y^2 = 1$ in an ellipse. Find the points on the ellipse that lie closest to and farthest from the origin.
- 17. Find the area of the region enclosed by $x + y^2 = 0$ and $x + 3y^2 = 2$.
- 18. The region bounded by $y = x^2$, y = 2-x, x = 0 for $x \ge 0$ revolves about y axis. Find the volume of the solid generated by shell method.

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- 19. Find the area of the region cut from the first quadrant by the cardioid $r = 1 + \sin \theta$
- 20. Evaluate the integral by changing the Cartesian integrals to polar integrals

$$\int_{-1}^{1} \int_{-\sqrt{1-y^2}}^{\sqrt{1-y^2}} (x^2 + y^2) \, dx \, dy$$

 $(5 \times 5 = 25)$

PART - C

Answer any three questions. Each question carries 10 marks.

21.

- (a) Find the critical point of $f(x) = x^3 12x 15$. Identify the intervals on which f is increasing and decreasing.
- (b) Show that the function $h(\theta) = 3\cos\frac{\theta}{2}$, $0 \le \theta \le 2\pi$ at $\theta = 0$ and $\theta = 2\pi$ have local extreme values at the given values of θ and say which kind of local extreme the function has.
- 22. Find the absolute maximum and minimum values of $f(x, y) = 2 + 2x + 2y x^2 y^2$ on the triangular region in the first quadrant bounded by the lines x = 0, y = 0, y = 9 x.
- 23. Find the volume of the solid generated by revolving the triangle with vertices (1,1), (1,2), (2,2) about
 - (i) the line x = 10/3.
 - (ii) the line y = 1
- 24. Find the volume of the region enclosed by the surfaces $z = x^2 + 3y^2$ and $z = 8 x^2 y^2$

 $(10 \times 3 = 30)^{-1}$
