

Reg. No .....

Name .....

19P4047

**MSc DEGREE END SEMESTER EXAMINATION - MARCH/APRIL 2019**

**SEMESTER 4 : MATHEMATICS**

**COURSE : 16P4MATT20EL : NUMERICAL ANALYSIS**

*(For Regular - 2017 Admission and Supplementary - 2016 Admission)*

Time : Three Hours

Max. Marks: 75

**Section A**

**Answer all the following (1.5 marks each)**

1. Evaluate the sum  $S = \sqrt{3} + \sqrt{5} + \sqrt{7}$  to 4 significant digits and find its absolute and relative error.
2. State Taylor's series and Maclaurin's series for a function.
3. Find the relative error of the number 9.6 if both of its digits are correct.
4. Define ill-conditioned matrix.
5. Establish whether the following matrix is singular, ill conditioned or well conditioned  
$$\begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9.1 \end{bmatrix}.$$
6. Show that  $e^x(u_0 + x\Delta u_0 + (x^2/2!)\Delta^2 u_0 + \dots) = u_0 + u_1 x + u_2(x^2/2!) + \dots$
7. Define  $[x_0, x_1, x_2]$
8. Evaluate  $\Delta(x+1)(x+2)$
9. Evaluate  $\Delta(\tan^{-1} x)$ .
10. From the Taylor series for  $y(x)$ , find  $y(0.1)$  if the function satisfies  $y' = x - y^2$  and  $y(0) = 1$ .

**(1.5 x 10 = 15)**

**Section B**

**Answer any 4 (5 marks each)**

11. Briefly explain Newton - Raphson method and using it find the root of the equation  $x = e^{-x}$
12. Use the method of iteration to find a real root of the equation  $x^3 + x^2 - 1 = 0$  on the interval  $[0,1]$  with an accuracy of  $10^{-4}$ .
13. Discuss the method of Tridiagonal system.
14. Using Newton's difference formula. Find the sum  $S_n = 1^3 + 2^3 + \dots + n^3$

15. Applying Lagrange's formula, find a cubic polynomial which approximates the following data:
- |      |     |    |   |   |
|------|-----|----|---|---|
| x    | -2  | -1 | 2 | 3 |
| F(x) | -12 | -8 | 3 | 5 |
16. Determine the value of y when x = 0.1 given that y(0)=1 and  $y' = x^2 + y$  using modified Euler's method with h = 0.05.

**(5 x 4 = 20)**

### Section C

**Answer any 4 (10 marks each)**

- 17.1. a) Let  $x = \epsilon$  be a root of  $f(x)=0$  and let I be the interval containing the point  $x = \epsilon$ . Let  $\phi(x)$  and  $\phi'(x)$  be continuous in I where  $x = \phi(x)$  is equivalent to  $f(x) = 0$ . Then if  $|\phi'(x)| < 1$  for all x in I, the sequence of approximations  $x_0, x_1, \dots, x_n$  defined by  $x_{n+1} = \phi(x_n)$  converges to the root  $\epsilon$ , provided the initial approximation is chosen in I. b) Find a root of the equation  $\sin x = 1 - x$  using Ramanujan's method.

**OR**

2. Describe Gauss Jordan method and solve the equations  $5x-2y+z = 4$ ,  $7x+y-5z = 8$ ,  $3x+7y+4z = 10$ .
- 18.1. Explain the method to solve Linear systems using iterative methods.

**OR**

2. Explain the errors in Numerical differentiation and hence find the error obtained in first and second derivative at  $x = 1.6$ , for the function which fits the data : (1, 2.7183), (1.2, 3.3201), (1.4, 4.0552), (1.6, 4.9530), (1.8, 6.0496), (2, 7.3891), (2.2, 9.0250).
- 19.1. Derive Newton's general interpolation formula with divided differences.

**OR**

2. Solve the initial value problem  $y' = 3x + y/2$  with the condition  $y(0)=1$ . Find  $y(0.2)$  and  $h=0.05$ .
- 20.1. Use Runge - Kutta method to solve  $10y' = x^2 + y^2, y(0)=1$ , for the interval  $0 < x \leq 0.4$  with  $h = 0.1$ .

**OR**

2. Derive the predictor - corrector formula using Newton's backward and forward difference interpolation formula.

**(10 x 4 = 40)**