

B. Sc. DEGREE END SEMESTER EXAMINATION - OCTOBER 2018**SEMESTER - 3: MATHEMATICS****(CORE COURSE FOR B. Sc. MATHEMATICS AND B. Sc. COMPUTER APPLICATIONS)****COURSE : 15U3CRMAT3-15U3CRCMT3, CALCULUS***(For Regular - 2017 Admission and Supplementary / Improvement 2016, 2015, 2014 Admissions)*

Time : Three Hours

Max Marks : 75

PART - AAnswer **all** questions. Each question carries 1 mark.

1. Find the nth derivative of $\sin(ax+b)$
2. State Taylor's theorem
3. What is the relation between the evolute and envelope of a curve
4. Find $\partial f / \partial x$ if $f(x,y) = \sin(xy)$
5. Find the critical points of $f(x,y) = xy$
6. Evaluate $\int_0^{\pi/4} \tan x \sec^2 x \, dx$
7. What is the length of the smooth curve $x=g(y)$ from $y=c$ to $y=d$
8. State Pappus theorem for volumes
9. Evaluate $\int_0^3 \int_0^2 (4 - y^2) \, dy \, dx$
10. What is described by $r = a$ in cylindrical co-ordinates (1 x 10 = 10)

PART - BAnswer **any 8** questions. Each question carries 2 marks.

11. If $x = a \cos \theta$, $y = b \sin \theta$ show that $y_2 = b/a^2 \operatorname{cosec}^3 \theta$
12. Find the envelope of $\frac{x}{a} + \frac{y}{a-a} = 1$, where a is a constant
13. If $w = e^x + x \log y + y \log x$ show that $w_{yx} = w_{xy}$
14. If $u = x^2 + y^2$, $x = \cos t$, $y = \sin t$, find $\frac{du}{dt}$
15. Draw a tree diagram for the chain rule for functions of 3 variables
16. Find the length of the curve $x = 1 - t$, $y = 2 + 3t$, $-2/3 \leq t \leq 1$
17. Find the area of the region enclosed by $x = 2y^2$, $x = 0$, $y = 3$
18. Write an equivalent integral with the order of integration reversed for $\int_0^1 \int_1^{e^x} dy \, dx$
19. Find a spherical co-ordinate equation for the cone $z = \sqrt{x^2 + y^2}$
20. Evaluate $\int_1^e \int_1^e \int_1^e \frac{1}{xyz} \, dx \, dy \, dz$

(2 x 8 = 16)

PART - C

Answer **any 5** questions. Each question carries 5 marks.

21. Prove that $\tan^{-1} x = x - \frac{x^3}{3} + \frac{x^5}{5} - \dots$
22. Find the centre of curvature of $y^2=4ax$
23. If $w=\tan^{-1} \frac{x}{y}$, $x=ucosv$, $y=usinv$ find $\frac{\partial w}{\partial u}$ and $\frac{\partial w}{\partial v}$
24. Find the area between the curves $x + y^2 = 0$ and $x + 3y^2 = 2$
25. Find the surface area of the cone generated by revolving the line segment $y = \frac{x}{2}$, $0 \leq x \leq 4$ about the x-axis
26. Find the area of the cardioid $r = a (1 + \cos \theta)$
27. Evaluate $\int_0^{2\pi} \int_0^\pi \int_0^{\frac{1-\cos\phi}{2}} \rho^2 \sin\phi d\rho d\phi d\theta$

(5 x 5 = 25)

PART - D

Answer **any 2** questions. Each question carries 12 marks

28. a) If $y=e^{\tan^{-1} x}$, prove that $(1+x^2) y_{n+1} + 2n(x-1) y_n + m(n-1)y_{n-1}=0$
 b) Find the asymptotes of $y^3-6xy^2+11x^2y-6x^3+x+y=0$
29. Find the absolute maximum and minimum values of $f(x,y) = 2x^2-4x+y^2-4y+1$ on the closed region in the first quadrant bounded by $x=0, y=2, y=2x$
30. a) The region bounded by the curve $y = x^2$, the line $y = 2 - x$ and the y- axis for $x \geq 0$ is revolved about the y-axis to generate a solid. Find the volume of the solid using shell method
 b) Find the length of the curve $y = \frac{1}{3} (x^2 + 3)^{3/2}$ from $x=0$ to $x=3$
31. Evaluate $\int_0^3 \int_0^4 \int_{\frac{y}{2}}^{\frac{y}{2}+1} (\frac{2x-y}{2} + \frac{z}{3}) dx dy dz$ by applying the transformation $u = \frac{2x-y}{2}$, $v = \frac{y}{2}$, $w = \frac{z}{3}$ and integrating over an appropriate region in uvw-space

(12 x 2 = 24)
