B. Sc. DEGREE END SEMESTER EXAMINATION OCTOBER 2017

SEMESTER – 3 : CORE COURSE FOR MATHEMATICS AND COMPUTER APPLICATIONS COURSE: 15U3CRMAT3-15U3CRCMT3; CALCULUS

(For Regular - 2016 Admission and Supplementary / Improvement 2015 & 2014 Admission)

Time: Three Hours

Max Marks: 75

PART A

Answer all questions. Each question carries 1 mark

- 1. Expand $\log (a + x)$ by Taylor's theorem.
- 2. Find the n^{th} derivative of $y = a^{mx}$.
- 3. Define envelope of a one parameter of family of curves.
- 4. Show that $f(x, y, z) = x^2 + y^2 2z^2$ satisfies Laplace equation.
- 5. Define critical point of a function f(x, y).
- 6. Find the length of the curve $x = \cos t$, $y = t + \sin t$, $0 \le t \le \pi$
- 7. Write surface area formula for revolution about y axis.
- 8. Find the volume of the solid generated by revolving the region $y = x^2$, y = 0, x = 2.
- 9. Find a spherical coordinate equation for the cone $z = \sqrt{(x^2 + y^2)}$.
- 10. Find the area of the region *R* bounded by y = x + 2 and $y = x^2$ using double integrals.

 $(1 \times 10 = 10)$

PART B

Answer any eight questions. Each question carries 2 mark

- 11. Find the radius of curvature of the cycloid x = a (t + sint), y = a (1 cost).
- 12. Determine the points of inflexion of the curve $y = x^4 6x^3 + 12x^2 + 5x + 7$.
- 13. Find all second order partial differential equation of the function f(x, y) = x + y + xy.
- 14. Find dw/dt if w = xy + z, $x = \cos t$, $y = \sin t$, z = t.
- 15. Express w_r and w_s in terms of r and s if $w = x + 2y + z^2$, x = r/s, $y = r^2 + \ln s$, z = 2r.
- 16. Find the length of the curve $y = (1/3)(x^2 + y^2)^{3/2}$ from x = 0 to x = 3.
- 17. Find the area of surface of the region generated by revolving the curve $x = y^3/3$, $0 \le y \le 1$ about x axis.
- 18. Find the limits of integration for integrating $f(r, \theta)$ over the region *R* that lies inside the cardioid $r = 1 + \cos\theta$ and outside the circle r = 1.
- 19. Evaluate the cylindrical coordinate integral $\int_0^{2\pi} \int_0^3 \int_{\frac{r^2}{3}}^{\sqrt{18-r^2}} dz \, r \, dr \, d\theta$.
- 20. Reverse the order of integration, and evaluate the integral $\int_0^{\pi} \int_x^{\pi} \frac{\sin y}{y} dy dx$.

 $(2 \times 8 = 16)$

PART C

Answer any five questions. Each question carries 5 mark

- 21. Find all the asymptotes of the curve x^{3} $x^{2}y xy^{2} + y^{3} + 2x^{2} 4y^{2} + 2xy + x + y + 1 = 0$.
- 22. Obtain the evolute of the parabola $y^2 = 4ax$.
- 23. Find the absolute maximum and minimum values of $f(x, y) = 2 + 2x + 2y x^2 y^2$ on the triangular region in the first quadrant bounded by the lines x = 0, y = 0, y = 9 x.
- 24. Find the volume of the solid generated by revolving the region between the parabola $x = y^2 + 1$ and the line x = 3 about the line x = 3.
- 25. Find the volume of the solid generated by the region bounded by the curve $y = x^2 + 1$ and the line y = -x + 3 is revolved about the x axis.
- 26. Find the volume using triple integrals of the region in the first octant bounded by the cordinate planes and the surface $z = 4 x^2 y$.

27. Evaluate the integral
$$\int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \int_{csc\phi}^{2} 5\rho^{4} \sin^{3}\phi \, d\phi d\theta d\rho.$$

 $(5 \times 5 = 25)$

PART D

Answer any two questions. Each question carries 12 mark.

- 28. Find the nth derivative of $y = cos(m sin^{-1}x)$ for x = 0.
- 29. Find the points closest to the origin on the hyperbolic cylinder $x^2 z^2 1 = 0$.
- 30. a. Find the length of the curve y = (x/2)^{2/3} from x = 0 to x = 2.
 b. Find the surface area of the cone frustum generated by revolving the line segment y = (x/2) + (1/2), 1 ≤ x ≤ 3 about the y axis.
- 31. Let *D* be the region bounded below by the cone $z = \sqrt{x^2 + y^2}$ and above by the plane z = 1. Set up the triple integrals in spherical coordinates that give the volume of *D* using the following orders of integration.
 - a) $d\rho d\phi d\theta$
 - b) $d\phi d\rho d\theta$

(12 x 2 = 24)
