Reg. No	Name:
neg. No	Name:

## MSC DEGREE END SEMESTER EXAMINATION 2014 -15 SEMESTER -1: CHEMISTRY COURSE: P1CHET03/P1CPHT03 - QUANTUM CHEMISTRY AND GROUP THEORY

Time: 3 Hrs. Max. Marks: 75

## **Section A**

Answer any **10** questions.

- 1. What is a state function? What are the conditions required for a state function to represent a visible physical state?
- 2. What do you mean by polar plot? Draw one polar plot.
- 3. Write wave functions for a simple harmonic oscillator corresponding to v = 0 and v = 1 state. Represent it graphically.
- 4. Write Rodrigue's formula. Explain the significance.
- 5. What are spherical harmonics? Write first two spherical harmonics.
- 6. State and explain the postulate of spin by Uhlenbeck.
- 7. Distinguish between reducible and non-reducible representation with examples.
- 8. What is a cyclic group? Give an example.
- 9. Find the direct product  $E_g \times A_u$  in  $C_{2h}$ . Use  $C_{2h}$  character table in Question No.21.
- 10. Reduce the representation (6  $\,$  0  $\,$  -2). Use  $C_{3v}$  character table in Ouestion No.25.
- 11. What are vanishing and non vanishing integrals?
- 12. Define "normal modes of vibration".
- 13. State Laporte selection rules for centrosymmetric systems.

 $(10 \times 2 = 20)$ 

## **Section B**

Answer any **5** questions.

- 14. Assume a particle confined to a three-dimensional box having dimensions:
  - (i) a = b = c, (ii)  $a = b \neq c$ . Given the quantum number values of 1 and
  - 2. Calculate energies for levels  $E_{211}$ ,  $E_{121}$ ,  $E_{122}$  and  $E_{212}$  and comment on its degeneracy, if any.
- 15. Show that Hermitian operators always have real eigen values.
- 16. Write a note on tunnelling effect.
- 17. Discuss the Stern Gerlach experiment and the corresponding inferences.
- 18. What is similarity transformation? Illustrate using suitable example.
- 19. Find E x E. Reduce it into its IR components. Use  $C_{3\nu}$  character table in Question No.25.
- 20. Generate matrices for  $C_3$  and  $\sigma_h$  and show that their product is an  $S_3$ .

21. Using Cartesian coordinates find out the normal modes of vibrations in  $N_2F_2$ . Identify the Raman active vibrations. Use  $C_{2h}$  character table.

$C_{2h}$	E	$C_2$	i	$\sigma_{h}$			
$A_g$	1	1	1	1	R <sub>x</sub>	$x^{2}, y^{2}, z^{2},$	
						xy	
$E_{a}$	1	-1	1	-1	$R_{z}$ , $R_{v}$	XZ, YZ	
$A_{u}$	1	1	-1	-1	$\begin{array}{c} R_{z,} \; R_{y} \\ z \end{array}$		
$B_u$	1	-1	-1	1	x, y		
	•			·	-		$(5 \times 5 = 25)$

## **Section C**

Answer any 2 questions.

- 22. Set up the Schrodinger equation for hydrogen atom. Separate the variables and obtain the solution for the *phi* equation.
- 23. Discuss the ladder operator method to obtain the eigen values for angular momentum.
- 24. Using Great orthogonality theorem derive C<sub>4v</sub> character table.
- 25. Find IR and Raman active vibrations in NH<sub>3</sub>. Use C<sub>3v</sub> character table.

$C_{3v}$   E $2C_3$ $3\sigma_v$	
C <sub>3</sub> V   L 2C <sub>3</sub> 3O <sub>V</sub>	
$A_1$ 1 1 z $x^2+y^2, z^2$	
$A_2 \mid 1  1  -1 \mid R_z \mid$	
E 2 -1 0 $(x,y) (R_x, (x^2-y^2, x^2-y^2))$	
$R_y$ ) xy) (xz,	
yz)	
(2 x	15 = 30)

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