M A DEGREE END SEMESTER EXAMINATION 2014 -15 SEMESTER -1: ECONOMICS COURSE: P1ECOT05 - QUANTITATIVE TECHNIQUES FOR ECONOMIC ANALYSIS - I

Time: 3 Hours

Maximum: 75 Marks

Part A

Answer **all** questions

1. What are the important laws of matrix addition? Give examples.

- 2. Define CES production function.
- 3. What do you mean by linearly homogeneous functions?
- 4. State any two basic rules of integration. Give examples.
- 5. Define basic feasible solution.

 $(5 \times 2 = 10)$

Part B Answer any **Seven** of the Followings

6. Given
$$A = \begin{bmatrix} 2 & 4 \\ -1 & 3 \end{bmatrix}$$
, $B = \begin{bmatrix} 3 & 8 \\ 0 & 1 \end{bmatrix}$ and $C = \begin{bmatrix} 1 & 0 & 9 \\ 6 & 1 & 1 \end{bmatrix}$ then show that
(a) $(A+B)^{T} = A^{T} + B^{T}$ (b) $(AC)^{T} = C^{T}A^{T}$

7. Show that $\begin{vmatrix} b+c & a & a \\ b & c+a & b \\ c & c & a+b \end{vmatrix} = 4abc$.

- 8. Explain input-output model and its solution in detail.
- 9. Discuss the economic application of partial differentiation on elasticity and demand.
- 10. Evaluate the first and second-order partial derivatives of $u = (x^2 + 2xy y^2)e^x$ and verify that the order of partial derivation is immaterial.

11. Find the total differential of the function $y = \frac{x_1 + x_2}{2x_1^2}$.

12. Show that $z = (x^2 + y^2)e^{x^2 - y^2}$ has a minimum value at x = y = 0.

13. Integrate the following functions

(i)
$$\frac{4x}{x^2 + 1}$$
 (ii) $4x \exp(x^2 + 3)$

- 14. Explain the Big-M method of finding solution to a LPP.
- 15. What do you mean by duality in LPP? Discuss its interpretation.

 $(5 \times 7 = 35)$

Part C Answer any **Two** of the following

16. Find the solution of the equation system

$$7x_1 - x_2 - x_3 = 0$$

$$10x_1 - 2x_2 + x_3 = 8$$

$$6x_1 + 3x_2 - 2x_3 = 7$$

17. A firm has the following total-cost and demand functions

$$C = \frac{1}{3}Q^3 - 7Q^2 + 111Q + 50$$

$$O = 100 - P$$

What is the maximum profit?

18. Solve the following linear programming problem by the simplex method Maximize $Z = 6x_1 + 2x_2 + 5x_3$

subject to
$$\begin{bmatrix} 2 & 3 & 1 \\ 1 & 0 & 2 \\ 1 & 2 & 5 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} \le \begin{bmatrix} 10 \\ 8 \\ 19 \end{bmatrix}$$

and $x_1, x_2, x_3 \ge 0$.

 $(2 \times 15 = 30)$
