

Reg. No.....Name.....

**M.SC DEGREE END SEMESTER EXAMINATION OCTOBER 2016**  
**SEMESTER - 3: PHYSICS**

**COURSE: P3PHYT10 - COMPUTATIONAL PHYSICS**

Common for Regular (2015 Admission) & Supplementary / Improvement (2014 Admission)

Time: Three Hours

Max. Marks: 75

**PART A (Objective)**

(Answer **all** questions. Each question carries 1 Mark)

- .....Interpolation formula can be used whether the values of x are equally spaced or not  
 (a) Newtons forward (b) Newtons backward (c) Newtons central difference (d) Lagrange's
- If all the points of observations lie on the curve ,then by least square method E will be  
 (a) Zero (b) positive (c) negative (d) all of these
- The error in Simpsons 1/3 rule is---  
 (a)  $3/80 h^5 y^7(x)$  (b)  $b-a/80 h^4 y^4$  (c)  $4h^7/98 h^4 y^3(x)$  (d)  $-(b-a)/180 h^4 y^4 (\bar{x})$
- "Multi step method "is also known as -----  
 (a) Predictor corrector method (b) R-K method (c) Milnes method (d) Eulers method
- A method in which the computation of many present unknown values necessitates the solution of a set of simultaneous equations is called --  
 (a) Explicit method (b) implicit method (c) real method (d)direct method

(1 x 5 = 5)

**Part B (Short Answer)**

(Answer **any five** question. Each question carries 2 mark)

- Show that the operations  $\mu$  and E commute
- What is  $\Psi^2$  test
- What is double integration
- What are the errors associated numerical differentiation
- Derive the Schmidt explicit formula from diffusion equation
- Explain the geometrical significance of trapezoidal rule
- Derive second order Runga-kutta formula from modified Euler method
- Evaluate  $I = \int_0^1 \frac{1}{1+x} dx$  using Simpsons 1/3 rule take  $h=1/6$

(2 x 5 = 10)

### PART C (Problem/Short Essay)

(Answer **any three** questions. Each question carries 4 Marks)

14. Use Gauss elimination to solve  $2x+y+z=10, 3x+2y+3z=18, x+4y+9z=16$

15. Evaluate  $f(3)$  using interpolating polynomial

X	:	1	2	5
f(x)	:	1	4	10

16. By the method of least squares fit a curve of the form  $y=a+bx+cx^2$  to the following data:

x :	0.0	0.5	1.0
y :	1.0000	1.6487	2.7183

17. Determine the largest Eigen value of the matrix and corresponding Eigen

	1	6	1
vector of the matrix	1	2	0
	0	0	3

18. Find  $y(2.0)$  if  $y(t)$  is the solution of  $\frac{dy}{dt} = \frac{1}{2}(t+y)$ ,  $y(0)=2$ ,  $y(0.5)=2.636$ ,  
 $y(1.0)=3.595$  and  
 $y(1.5) = 4.968$  using Milnes method.  
(4 x 3 = 12)

### Part D (Essay)

(Answer **all** question, 12 marks each)

19. (a) Tabulate the values of the function  $f(x,y)=x^2+y^2-y$ , for  $x=0,1,2,3,4$  and  $y=0,1,2,3,4$  using the table of values computer (2.5,3.5) by numerical double interpolation

**OR**

(b) Obtain the forward and backward difference polynomials from the following data and interpolate at  $x=0.25$  and  $x=0.35$

x	0.1	0.2	0.3	0.4	0.5
f(x)	1.40	1.56	1.76	2.00	2.28

20. (a) Discuss the concept of Romberg's integration and using it find the value of  $\int_1^{1.8} y(x) dx$

X	1.0	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8
Y	1.543	1.669	1.811	1.971	2.151	2.352	2.577	2.828	3.107

Do the iteration till  $m=3$

- (a) Find the approximate value of  $y = \int_0^{\pi} \sin x \, dx$  using (i) trapezoidal rule, (ii) Simpson's 1/3 rule by dividing the range of integration into six equal parts. Calculate the percentage error from its true value in both the cases.

21. (a) Use Runge-Kutta method of fourth order to solve numerically the initial value problem

$$10 \frac{dy}{dx} = x^2 + y^2, \quad y(0) = 1 \quad \text{and find } y \text{ in the interval } 0 \leq x \leq 0.4 \text{ taking } h = 0.1$$

**OR**

- (b) Use Gauss-Jordan method to compute the inverse of the matrix

$$\begin{pmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 2 & -3 & 4 \\ 0 & -1 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 0 & -1 & 1 \end{pmatrix}$$

22. (a) Show that  $2\Delta x (\partial T / \partial x)_{i,j} = 3T_{i,j} - 4T_{i-1,j} + T_{i-2,j}$  using the basic concept in finite difference methods

**OR**

- (b) Explain Crank-Nicolson method and weighted average implicit method in detail (12 x 4 = 48)

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